# **Cryptography:**

Information confidentiality, integrity, authenticity, person identification

1976 m.

# Symmetric cryptography ------ Asymmetric cryptography

Asymmetric encryption Symmetric encryption:

E-signature - Public Key Infrastructure - PKI

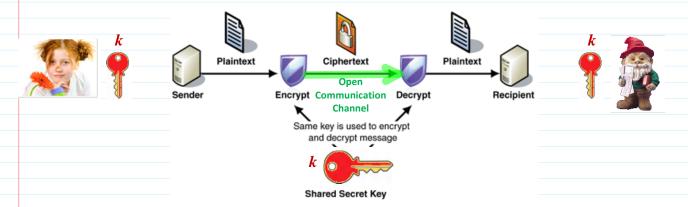
block ciphers E-money

stream ciphers E-voting H-functions, Message digest

Digital Rights Management - DRM Marlin HMAC H-Message Authentication Code

Etc.

# **Symmetric - Secret Key Encryption - Decryption**



Imagine that number of users of cryptosystem is 100.

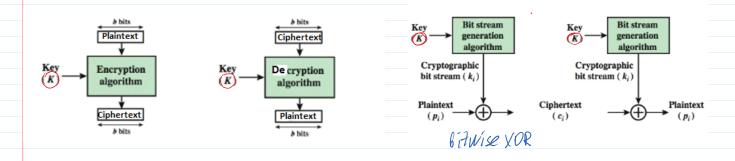
$$C_{100}^2 = \frac{100*99}{2} = 4950$$

Symmetric ciphers

AES: Block Ciphers

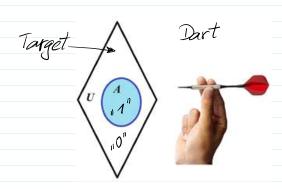
128, 196, 256

**Stream Ciphers** 



Vernam cipher (1917) - One Time Pad

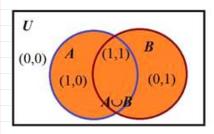
Logical operations

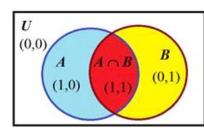


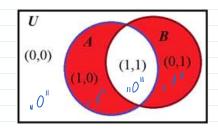
AUB

ANB

ADB





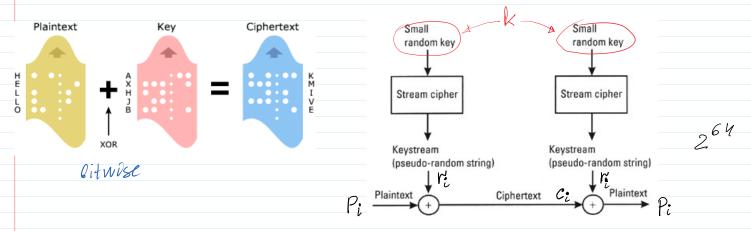


$$0^{n}$$
 No  $m \in \{0,1\}$   
 $k = rand \{0,1\}$ ;  $k \in \{0,1\}$   
 $c = m \oplus k$   $c$   
If  $Pr(k=0) = Pr(k=1) = 1/2$ 

If Pr(k=0) = Pr(k=1) = 1/2Then Pr(c=0) = Pr(c=1) = 1/2Pr(m=0) = Pr(m=1) = 1/2

B: 
$$c = m \oplus k - k = m$$
  
 $c \oplus k = m \oplus k \oplus k = m$   
 $= m \oplus 0 = m = 1$   
 $c \oplus k = m$ 

## Stream Cipher - Vernam Cipher - One-Time Pad



# **Stream Ciphers**



- To encrypt plaintext stream
  - A random set of bits is generated from a seed key, called keystream which is as long as the message
  - Keystream bits are added modulo 2 to plaintext to form the ciphertext stream
- To decrypt ciphertext stream
  - use the same seed key to generate the same keystream used in encryption
  - Add the keystream modulo 2 to the ciphertext to retrieve the plaintext
  - i.e.  $C = P \oplus K \Rightarrow C \oplus K = (P \oplus K) \oplus K = P$

**Pseudo Random Numbers Generators - PRNG** 

$$r_{i+1} = PRNG(r_i)$$
  $r_1 = PRNG(r_0)$ ;  $r_0 - initial value$ :  $r_0 = k$ .

 $r_2 = PRNG(r_1)$ 
 $r_1 = PRNG(r_2)$ 
 $r_2 = PRNG(r_3)$ 

**Vernam cipher**: Plaintext  $m \longrightarrow Encryption E_k(m) = c \longrightarrow Ciphertext c.$ 

For general encryption and decryption  $\frac{\mathsf{bitwise}}{\mathsf{bitwise}}$  XOR operation  $\bigoplus$  is used for bitstrings.

Plaintext m and key K (bit stream equal to m bit stream) are transformed to binary form consisting of bitstrings.

Encryption:  $c=m \oplus K$ .

Decryption:  $m = c \oplus K = m \oplus K \oplus K = m \oplus 0 = m$ .

Security requirements.

- 1.Key K must be generated at random using (Pseudo)Random Number Generators PRNG.
- 2. Key K bit length must be no less than plaintext bit length: |k| > = |m|.
- 3.Key K can be used only once.

Active adversary, Eavesdrapping adversary.

**Attention!** If the same agreed secret key K is used twice in Vernam cipher for any two messages  $m_1$  and  $m_2$  encryption, then *eavesdropping* adversary can obtain an data  $d_b$  which is equal to bitwise XOR between  $m_1$  and  $m_2$ . Let ciphertexts  $c_1$  and  $c_2$  are obtained by the following encryption with the same symmetric key K

$$c_1 = m_1 \oplus K$$

$$c_2 = m_2 \oplus K$$

where  $\bigoplus$  is bitwise XOR operation.

Then eavesdropping adversary computes the following data *d* 

 $d_b = c_1 \oplus c_2 = m_1 \oplus K \oplus m_2 \oplus K = m_1 \oplus m_2 \oplus K \oplus K = m_1 \oplus m_2 \oplus 0 = 0 = m_1 \oplus m_2$ . It is reckoned as a *crucial insecurity* since cryptanalysis of data  $d_b$  is significantly facilitated and both  $m_1$  and  $m_2$  can be disclosed.

Moreover, if any message of two  $m_1$  or  $m_2$  are revealed by some circumstances, say message  $m_2$ , then the other message  $m_1$  becomes clear to the adversary by computing

$$d_b \bigoplus m_2 = m_1 \bigoplus m_2 \bigoplus m_2 = m_1 \bigoplus 0 = m_1$$
.

**Never** use the same secret key *K* twice in Vernam cipher!

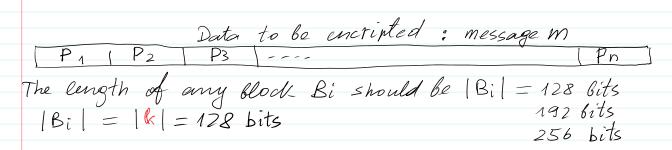
The same secret key K can be used multiple times in standardized block ciphers (AES) and stream ciphers.

>> kAB = int64(195681379) >> c1b=binaryxor(m1b,kb) kAB = 195681379 c1b = 1011101010000000100010100011 >> k=kAB >> c2b=binaryxor(m2b,kb) c2b = 1011101010011101110001101010 k = 195681379 >> kb=dec2bin(k) >> c12b=binaryxor(c1b,c2b) kb = 1011101010011101110001100011 c2b = 1011101010011101110001101010 >> m1=120000 >> c12b=binaryxor(c1b,c2b) c12b = 11101010011001001 m1 = 120000>> m12b=binaryxor(m1b,m2b) >> m1b=dec2bin(m1) m12b = 11101010011001001 m1b = 11101010011000000 >> m2=9 >> db=c12b m2 = 9db = 11101010011001001 >> m2b=dec2bin(m2) >> mm1b=binaryxor(db,m2b) m2b = 1001mm1b = 11101010011000000 >> mm1b=bin2dec(mm1b) mm1b = 120000

Block cipher AES - 128, 192, 256 --> Encryption --> Decryption

Advanced Encryption Standard ~ 2000

Key length 128, 192, 256, Bits: | k | € { 128 b, 192 b, 256 b }



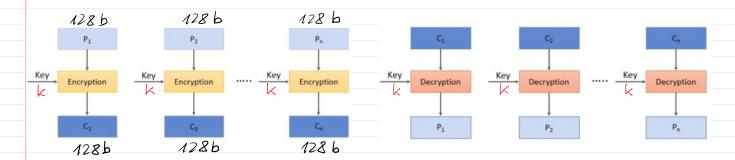
Block Cipher: Electronic Code Book -ECB mode of encryption

From <https://binaryterms.com/block-cipher.html>

### 1. Electronic Code Book (ECB) mode in AES-128

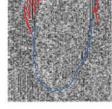
This is considered to be the easiest block cipher mode of operation. In electronic codebook mode (ECB) the plain text is divided into the blocks, each of 128-bit. Each block is encrypted one at a time to produce the cipher block. The same key is used to encrypt each block.

When the receiver receives the message i.e. ciphertext. This ciphertext is again divided into blocks, each of 128-bit and each block is decrypted independently one at a time to obtain the corresponding plain text block. Here also the same key is used to decrypt each block which was used to encrypt each block.

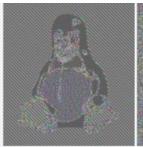


Enc 
$$AES(k, P_1) = C_1$$
  
 $ENCAES(k, P_2) = C_2$   
 $ENC AES(k, P_n) = C_n$ 











(a) plaintext

(b) plaintext encrypted in ECB mode using AES  $\,$ 

Original image

Encrypted using ECB mode

Modes other than ECB result in pseudo-randomness

https://binaryterms.com/block-cipher.htm

### 2. Cipher Block Chaining - CBC Mode

To overcome the limitation of ECB i.e. the repeating block in plain text produces the same ciphertext, a new technique was required which is Cipher Block Chaining (CBC) Mode. CBC confirms that even if the plain text has repeating blocks its encryption won't produce same cipher block.

To achieve totally different cipher blocks for two same plain text blocks **chaining** has been added to the block cipher. For this, the result obtained from the encryption of the first plain text block is fed to the encryption of the next plaintext box.

In this way, each ciphertext block obtained is dependent on its corresponding current plain text block input and all the previous plain text blocks. But during the encryption of first plain text block, no previous plain text block is available so a random block of text is generated called **Initialization vector**.

Now let's discuss the encryption steps of CBC

Step 1: The initialization vector and first plain text block are XORed and the result of XOR is then encrypted using the key to obtain the first ciphertext block.

Step 2: The first ciphertext block is fed to the encryption of the second plain text block. For the encryption of second plain text block, first ciphertext block and second plain text block is XORed and the result of XOR is encrypted using the same key in step 1 to obtain the second ciphertext block.

Similarly, the result of encryption of second plain text block i.e. the second ciphertext block is fed to the encryption of third plain text block to obtain third ciphertext block. And the process continues to obtain all the ciphertext blocks.

# **Decryption Steps:**

**Step 1:** The initialization vector is placed in the shift register. It is encrypted using the same key.

Keep a note that even in the **decryption process** the **encryption** algorithm is implemented instead of the decryption algorithm.

Then from the encrypted IV s bits are XORed with the s bits ciphertext C1 to retrieve s bits plain text P1.

IV A K=C10

Con = 11 & k

CBC
Cipher block
chaining
Encryption
parallelizable:
Decryption
Parallelizable:

111\_010 SymmetricEncryption CBC CTR Page 6

I nen trom the encrypted IV s bits are XUKEG WITH the S bits cipnertext CI to retrieve s bits plain text P1.

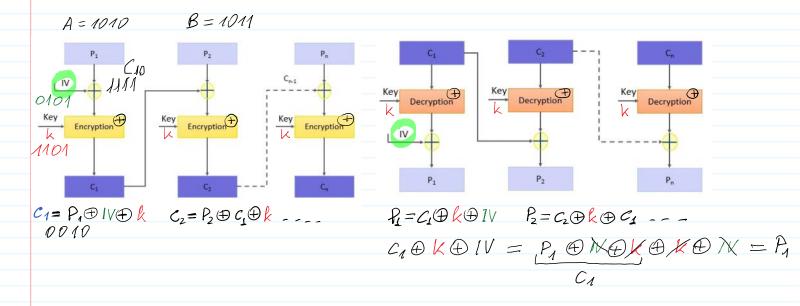
**Step 2:** The IV in the shift register is left-shifted by s bits and the s bits C1 replaces the rightmost s bits of IV.

The process continues until all plain text fragments are retrieved.

parallelizable:

Decryption Yes
parallelizable:

Random read Yes
access:



## https://binaryterms.com/block-cipher.html

#### 5. Counter Mode - CTR

It is similar to OFB but there is no feedback mechanism in counter mode.

Nothing is being fed from the previous step to the next step instead it uses a sequence of number which is termed as a **counter** which is input to the encryption function along with the key. After a plain text block is encrypted the counter value increments by 1.

Steps of encryption:

Step1: The counter value is encrypted using a key.

**Step 2:** The encrypted counter value is XORed with the plain text block to obtain a ciphertext block.

To encrypt the next subsequent plain text block the counter value is incremented by 1 and step 1 and 2 are repeated to obtain the corresponding ciphertext.

The process continues until all plain text block is encrypted.

Steps for decryption:

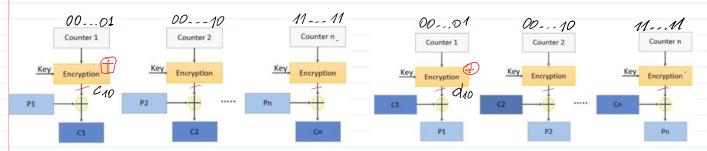
**Step1:** The counter value is encrypted using a key.

**Note:** Encryption function is used in the decryption process. The same counter values are used for decryption as used while encryption.

**Step 2:** The encrypted counter value is XORed with the ciphertext block to obtain a plain text block.

	CTR	
	Counter	
	Encryption parallelizable:	Yes
	Decryption parallelizable:	Yes
	Random read access:	Yes

### obtain a plain text block.



$$C_{10} = CTR_1 \oplus k$$

$$C_1 = C_{10} \oplus P_1$$

$$d_{10} = CTR_1 \oplus k$$

$$C_{10} = d_{10} = C_{10} \oplus P_1 \oplus CTR_1 \oplus k = =$$

$$= CTR_1 \oplus k \oplus P_1 \oplus CTR_1 \oplus k = P_1.$$

```
% AES128(in,kh32,NR,fun) Advanced Encryption Standard symmetric cipher with key length of 128 bits
               Encryption is performed for 1 block of length 128 bits or 16 ASCII symbols
%
% in - plaintext/ciphertext of string type: maximum 16 symbols or shorter
%
% kh32 - shared secret key in hexadecimal number of length=32 (128 bits)
% kh32 can be obtained when shared decimal key k is given using commands:
%
     >> k=int64(randi(2^28))
     k = 160966896
%
%
     >> kh32=dec2hex(k,32)
     kh32 = 000000000000000000000000099828F0
%
%
% NR - Number of Rounds (e.g. Nr = 10)
    The smaller NR, the lower security of encryption but the speed of encryption is higher
    The least number of NR is 1 and in this case security lack is evident
%
%
% fun - letter determining either encription: fun='e' or decryption: fun='d' functions
% Encryption example:
% >> in = 'Hello Bob';
% >> kh32 = '00000000000000000000000099828F0';
% >> NR = 10:
% >> Ch = AES128(in,kh32,NR,'e')
% ASCII e = ?1 \sim mV
                               % ciphertext in ASCII format
% Ch = 0f9a2c08d191310fb27ed16d90f45686 % ciphertext in hexadecimal format
%
% Decryption example:
% >> Dh = AES128(Ch,kh32,NR,'d')
% Dh = 00000000000048656c6c6f7720426f62 % decrypted message in hex format
% D = Hello Bob
                             % Decrypted message in ASCII format
%
```

function Out = AES128(in, key ,Nr, mode)

Encryption security depends of the number of rounds - NR

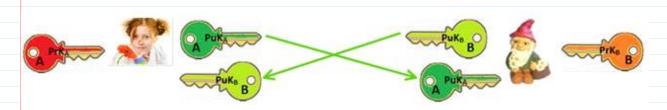
Test when NR=1

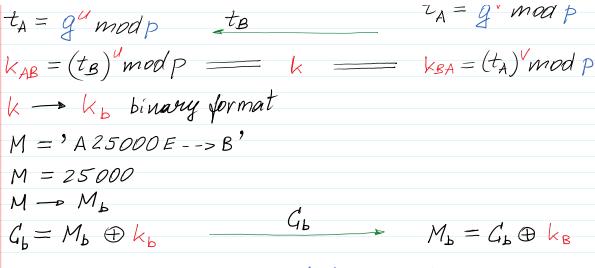
NR=10

And compare ciphertexts in hex format.

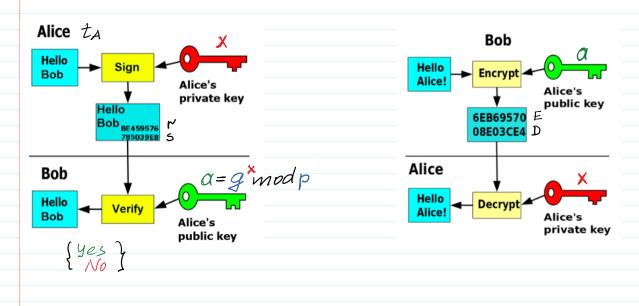
Till this place

# Asymmetric cryptography main actors and their credentials.





# Authenticated KAP - (AKAP)

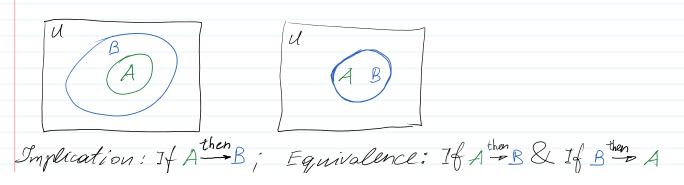


The reader confusing implication and equivalence operations (functions) can accept the following proposition as valid:

Till this place

if talker has a head and donkey has a head, then talker is a donkey.

To accept this proposition as valid means that thinker confuses notions of implication and equivalence. If reader is afraid to make such a mistake, we recommend to read about that in any external source.



Implication: If Athen B; Equivalence: If Athen B& If Bthen A
Implication: It A-B: Fauivalence: It A-B & If R-DA